

WHAT IS CLAIMED IS:

1. A method for designing a vehicle suspension system, comprising:
formalizing the vehicle suspension system by an equation (1), the vehicle
suspension system including a plurality of springs, a plurality of dampers each
5 corresponding to one of the springs, and a plurality p of actuators, equation (1) being a
linear matrix equation having a number, n, degrees of freedom, the linear matrix
equation including a damping matrix for viscous damping;

calculating eigenvectors of a stiffness matrix K of equation (1);

normalizing the eigenvectors with respect to a mass matrix M of equation (1);

10 calculating a similarity transform matrix S consisting of the normalized
eigenvectors; and

normalizing equation (1) using the similarity transform matrix S ,
wherein equation (1) is

$$M\dot{x}(t) + C(\dot{x}(t) - \dot{u}(t)) + K(x(t) - u(t)) = Pf(t)$$

15 wherein:

n and p respectively denote the degrees of freedom of the suspension system
and the number of independent actuators;

M , C , and K respectively denote a mass matrix, a damping matrix, and a
stiffness matrix, each of which is symmetrically $n \times n$, the mass matrix M being a
20 positive definite matrix, the damping matrix C being a positive semi-definite matrix,
and the stiffness matrix K being a positive definite matrix;

P denotes an $n \times p$ real matrix corresponding to positions of the actuators,

$x(t)$ and $u(t)$ respectively denote $n \times 1$ state and disturbance vectors; and

$f(t)$ denotes a $p \times 1$ external force vector.

25 2. The method of claim 1, wherein the normalizing equation (1) establishes a
proportional relationship $k_j = \alpha \times c_j$ between each pair of a spring coefficient k_j
of a j-th spring and a damping coefficient c_j of a j-th damper corresponding to the j-th
spring.

3. A vehicle suspension system comprising:
a plurality of springs;
a plurality of dampers, each corresponding to one of the springs; and
a plurality p of actuators for generating control force to the suspension system,

5 wherein:

the suspension system is formalized by an equation (1); and

equation (1) is decoupled into n modal equations,

wherein equation (1) is a linear matrix equation having a plurality n of degrees
of freedom, and the linear matrix equation includes a damping matrix for a viscous
10 damping,

wherein equation (1) is

$$M\ddot{x}(t) + C(\dot{x}(t) - \dot{u}(t)) + K(x(t) - u(t)) = Pf(t)$$

wherein:

n and p respective denote the degrees of freedom of the suspension system and
15 the number of independent actuators;

M , C , and K respectively denote a mass matrix, a damping matrix, and a
stiffness matrix, each of which is symmetrically $n \times n$, the mass matrix M being a
positive definite matrix, the damping matrix C being a positive semi-definite matrix,
and the stiffness matrix K being a positive definite matrix;

20 P denotes an $n \times p$ real matrix corresponding to positions of the actuators,

$x(t)$ and $u(t)$ respectively denote $n \times 1$ state and disturbance vectors; and

$f(t)$ denotes $p \times 1$ external force vector.

4. The vehicle suspension system of claim 3, wherein a proportional relationship
25 $k_j = \alpha \times c_j$ is satisfied between each pair of a spring coefficient k_j of a j -th
spring and a damping coefficient c_j of a j -th damper corresponding to the j -th spring.

5. The vehicle suspension system of claim 4, wherein the number n and the
number p are equal,

30 the suspension system further comprising:

a detecting unit for detecting at least one of the state vector $x(t)$ and its velocity $\dot{x}(t)$; and

a controller for controlling the actuators on the basis of the detected one of the state vector $x(t)$ or its velocity $\dot{x}(t)$,

5 wherein the controller controls the actuators by an actuating force of $f = Q^{-1} \hat{f}$,

wherein:

$Q = S^T P$, $\hat{f}_i = -C_{Si} \dot{\xi}_i$, and $x(t) = S \xi(t)$ are satisfied;

C_{Si} is a damping coefficient of a sky-hook damper connected to an i-th mode;

10 and

S is a matrix consisting of eigenvectors of the stiffness matrix K and is normalized with respect to the mass matrix M .

6. The vehicle suspension system of claim 4, wherein the number p is less than the number n,

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the suspension system further comprising:

a detecting unit for detecting at least one of the state vector $x(t)$ and its velocity $\dot{x}(t)$; and

a controller for controlling the actuators on the basis of the detected one of the state vector $x(t)$ or its velocity $\dot{x}(t)$,

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wherein the controller controls the actuators by an actuating force of

$f(t)$ that satisfies $\hat{f}_i = -F_{Si} \text{sign}(\dot{\xi}_i) = \sum_{j=1}^p Q_{ij} f_j$,

wherein:

$Q = S^T P$ and $x(t) = S \xi(t)$ are satisfied;

25 F_{Si} is a frictional force of a sky-hook coulomb friction damper connected to an i-th mode; and

S is a matrix consisting of eigenvectors of the stiffness matrix K and is normalized with respect to the mass matrix M .

7. The vehicle suspension system of claim 6, wherein the actuating force $f(t)$ satisfies

$$\left\{ \begin{array}{ll} \text{if } Q_{1j} \text{sign}(\dot{\xi}_1) \geq 0 \& Q_{2j} \text{sign}(\dot{\xi}_2) \geq 0 \& \dots Q_{nj} \text{sign}(\dot{\xi}_n) \geq 0, & f_j = -F_A \\ \text{if } Q_{1j} \text{sign}(\dot{\xi}_1) \geq 0 \& Q_{2j} \text{sign}(\dot{\xi}_2) \geq 0 \& \dots Q_{nj} \text{sign}(\dot{\xi}_n) < 0, & f_j = -F_1 \\ \vdots & \vdots \\ \text{if } Q_{1j} \text{sign}(\dot{\xi}_1) < 0 \& Q_{2j} \text{sign}(\dot{\xi}_2) < 0 \& \dots Q_{nj} \text{sign}(\dot{\xi}_n) \geq 0, & f_j = -F_{(2^n-2)} \\ \text{if } Q_{1j} \text{sign}(\dot{\xi}_1) < 0 \& Q_{2j} \text{sign}(\dot{\xi}_2) < 0 \& \dots Q_{nj} \text{sign}(\dot{\xi}_n) < 0, & f_j = -F_B \end{array} \right\}$$

with respect to $i = 1, \dots, n$ and $j = 1, \dots, p$,

wherein:

F_A is a value in a range of zero(0) to F_P ;

F_B is a value in a range of zero(0) to F_N ;

F_k for $k = 1, \dots, (2^n - 2)$ is a value between F_P and F_N ; and

F_P and F_N respectively denote a positive maximum force and a negative maximum force that a j-th actuator can generate.

8. The vehicle suspension system of claim 7, wherein the actuating force $f(t)$ satisfies

$$\left\{ \begin{array}{ll} \text{if } Q_{ij} \text{sign}(\dot{\xi}_i) \geq 0 \text{ for } i = 1, \dots, n, & f_j = -F_A \\ \text{if } Q_{ij} \text{sign}(\dot{\xi}_i) < 0 \text{ for } i = 1, \dots, n, & f_j = -F_B \\ \text{Otherwise,} & f_j = 0 \end{array} \right\}$$

with respect to $i = 1, \dots, n$ and $j = 1, \dots, p$.

9. The vehicle suspension system of claim 8, wherein values of F_A and F_P are equal, and values of F_B and F_N are equal.

10. A method for controlling a vehicle suspension system, the vehicle suspension including a plurality of dampers and a plurality of actuators, the vehicle suspension system being formalized by an equation (1) and being transformed to a decoupled equation (2), the method comprising:

calculating a velocity vector $\dot{x}(t)$ of a state vector $x(t)$ of equation (1);

calculating an actuating force $f(t)$ such that the actuating force $f(t)$

satisfies $f(t) = (S^T P)^{-1} (-C_{Si})(S^T K S)^{-1} (S^T K) \dot{x}(t)$, the C_{Si} being a damping coefficient of a sky-hook damper connected to an i-th mode; and

actuating the actuators by the calculated actuating force $f(t)$,

wherein:

equation (1) is

$$M\ddot{x}(t) + C(\dot{x}(t) - \dot{u}(t)) + K(x(t) - u(t)) = Pf(t), \text{ and}$$

equation (2) is

$$I\ddot{\xi}(t) + \text{diag}[2\zeta_i \omega_i] (\dot{\xi}(t) - \dot{\eta}(t)) + \Lambda_K (\xi(t) - \eta(t)) = \hat{f}(t)$$

wherein:

n and p respectively denote the degrees of freedom of the suspension system and the number of independent actuators;

M , C , and K respectively denote a matrix, a damping matrix, and a stiffness matrix, each of which is symmetrically $n \times n$, the mass matrix M being a positive definite matrix, the damping matrix C being a positive semi-definite matrix, and the stiffness matrix K being a positive definite matrix;

P denotes an $n \times p$ real matrix corresponding to positions of the actuators,

$x(t)$ and $u(t)$ respectively denote $n \times 1$ state and disturbance vectors;

$f(t)$ denotes a $p \times 1$ external force vector;

I is an $n \times n$ unit matrix;

S is a matrix consisting of eigenvectors of the stiffness matrix K and is normalized with respect to the mass matrix M ; and

$$Q = S^T P, \hat{f} = Qf(t), x(t) = S \xi(t), u(t) = S\eta(t),$$

$S^T K S = \text{diag}[\omega_i^2] = \Lambda_K$, and $S^T C S = \hat{C} = \text{diag}[2\zeta_i \omega_i]$ are satisfied by the matrix S .

11. A method for controlling a vehicle suspension system, the vehicle suspension including a plurality of dampers and a plurality of actuators, the vehicle suspension system being formalized by an equation (1) and being transformed to a decoupled equation (2), the method comprising:

calculating a velocity vector $\dot{x}(t)$ of a state vector $x(t)$ of equation 1;

calculating an actuating force $f(t)$ such that the actuating force $f(t)$

satisfies

$$\left\{ \begin{array}{ll} \text{if } Q_{1j} \text{sign}(\dot{\xi}_1) \geq 0 \& Q_{2j} \text{sign}(\dot{\xi}_2) \geq 0 \& \dots \& Q_{nj} \text{sign}(\dot{\xi}_n) \geq 0, & f_j = -F_A \\ \text{if } Q_{1j} \text{sign}(\dot{\xi}_1) \geq 0 \& Q_{2j} \text{sign}(\dot{\xi}_2) \geq 0 \& \dots \& Q_{nj} \text{sign}(\dot{\xi}_n) < 0, & f_j = -F_1 \\ \vdots & \vdots \\ \text{if } Q_{1j} \text{sign}(\dot{\xi}_1) < 0 \& Q_{2j} \text{sign}(\dot{\xi}_2) < 0 \& \dots \& Q_{nj} \text{sign}(\dot{\xi}_n) \geq 0, & f_j = -F_{(2^n-2)} \\ \text{if } Q_{1j} \text{sign}(\dot{\xi}_1) < 0 \& Q_{2j} \text{sign}(\dot{\xi}_2) < 0 \& \dots \& Q_{nj} \text{sign}(\dot{\xi}_n) < 0, & f_j = -F_B \end{array} \right\}$$

with respect to $i = 1, \dots, n$ and $j = 1, \dots, p$; and

actuating the actuators by the calculated actuating force $f(t)$,

wherein:

F_A is a value in a range of zero (0) to F_P ;

F_B is a value in a range of zero (0) to F_N ;

F_k for $k = 1, \dots, (2^n - 2)$ is a value between F_P and F_N ;

F_P and F_N respectively denote a positive maximum force and a negative

maximum force that a j-th actuator can generate;

equation (1) is

$$M\ddot{x}(t) + C(\dot{x}(t) - \dot{u}(t)) + K(x(t) - u(t)) = Pf(t); \text{ and}$$

equation (2) is

$$I\ddot{\xi}(t) + \text{diag}[2\zeta_i\omega_i](\dot{\xi}(t) - \dot{\eta}(t)) + \Lambda_K(\xi(t) - \eta(t)) = \hat{f}(t)$$

wherein:

n and p respective denote the degrees of freedom of the suspension system and the number of independent actuators;

M , C , and K respectively denote a mass matrix, a damping matrix, and a stiffness matrix, each of which is symmetrically $n \times n$, the mass matrix M being a positive definite matrix, the damping matrix C being a positive semi-definite matrix, and the stiffness matrix K being a positive definite matrix;

P denotes an $n \times p$ real matrix corresponding to positions of the actuators,

$x(t)$ and $u(t)$ respectively denote $n \times 1$ state and disturbance vectors;

$f(t)$ denotes a $p \times 1$ external force vector;

I is an $n \times n$ unit matrix;

S is a matrix consisting of eigenvectors of the stiffness matrix K and is normalized with respect to the mass matrix M ; and

$$Q = S^T P, \hat{f} = Qf(t), x(t) = S \xi(t), u(t) = S \eta(t),$$

$S^T K S = \text{diag}[\omega_i^2] = \Lambda_K$, and $S^T C S = \hat{C} = \text{diag}[2\zeta_i\omega_i]$ are satisfied by the matrix S .

12. The method of claim 11, wherein the actuating force $f(t)$ satisfies

$$\left\{ \begin{array}{l} \text{if } Q_{ij} \text{sign}(\dot{\xi}_i) \geq 0 \text{ for } i=1, \dots, n, \quad f_j = -F_A \\ \text{if } Q_{ij} \text{sign}(\dot{\xi}_i) < 0 \text{ for } i=1, \dots, n, \quad f_j = -F_B \\ \text{Otherwise,} \quad f_j = 0 \end{array} \right\}$$

with respect to $i = 1, \dots, n$ and $j = 1, \dots, p$.

13. The method of claim 12, wherein values of F_A and F_P are equal, and values of F_B and F_N are equal.